### Lecture 14. Lidar Data Inversion and Sensitivity Analysis

- Data inversion process
- Nonlinearity of PMT and discriminator
- More considerations for Na Doppler lidar
- Definition of sensitivity
- Summary
- Office demonstration



### Preprocess Procedure for Na Doppler Lidar

- Read data: for each set, and calculate T, W, and n for each set
- PMT/Discriminator saturation correction
- Chopper correction
- Background estimate and subtraction
- Range-dependence removal (not altitude)
- 🖵 Base altitude adjustment
- Take Rayleigh signal @ z<sub>R</sub> (Rayleigh fit or Rayleigh sum)
- Rayleigh normalization

$$N_N(\lambda, z) = \frac{N_S(\lambda, z) - N_B}{N_S(\lambda, z_R) - N_B} \frac{z^2}{z_R^2}$$





For small input photon flux, PMT output photon counts are proportional to the input photon counts:

$$\lambda_{oP} = \lambda_S = \lambda_i \eta_{QE}$$

When the input photon flux is considerably large, the output photon counts are no longer linear with input photons. Nonlinearity of PMT occurs:

$$\lambda_{oP} = \lambda_{S} e^{-\lambda_{S} \tau_{P}}$$

A discriminator is used to judge real photon signals and also has a saturation effect, i.e., its output photon counts are smaller than input photon counts when input count rate is large:  $\lambda$ 

$$\lambda_o = \frac{\lambda_{iD}}{1 + \lambda_{iD}\tau_d}$$

Since PMT output is the input of discriminator

$$\lambda_{iD} = \lambda_{oP}$$

we obtain

$$\lambda_{o} = \frac{\lambda_{S} e^{-\lambda_{S} \tau_{p}}}{1 + \lambda_{S} \tau_{d} e^{-\lambda_{S} \tau_{p}}} = \frac{\lambda_{S} e^{-\lambda_{S} \tau_{p}}}{1 + \lambda_{S} \tau_{d} e^{-\lambda_{S} \tau_{p}}}$$

where

 $\lambda_S = \lambda_i \eta_{QE}$   $\eta_{QE}$  is the quantum efficiency of cathode

Maximum output count rate is reached when  $\lambda_S = 1/\tau_p$ 

$$\lambda_{o\max} = \frac{1}{\tau_p e + \tau_d} \qquad \longrightarrow \quad \tau_p = \frac{\frac{1}{\lambda_{o\max}} - \tau_d}{e}$$





#### More Considerations

□ PDA frequency offset: usually nonzero, so must be taken into account. For AR1102 data, the freq offset is 10.27MHz.

Actual laser freq = CW laser freq + PDA freq offset

Binning, smoothing, or temporal integration in order to improve the signal-to-noise ratio (SNR).

More considerations will be shown in our office demonstration.

#### Sensitivity for T and W

The temperature and wind sensitivities are defined as



# Summary

Lidar data inversion is to convert raw photon counts to meaningful physical parameters like temperature, wind, number density, and volume backscatter coefficient. It is a key step in the process of using lidar to study science.

□ The basic procedure of data inversion originates from solutions of lidar equations, in combination with detailed considerations of hardware properties and limitations as well as detailed considerations of light propagation and interaction processes.

□ The data inversion procedure consists of three main processes: (1) preprocess, (2) process of T and  $V_R$ , (3) process of  $n_c$  and  $\beta$ , etc.

# Summary

□ The preprocess is to convert the raw photon counts to corrected and normalized photon counts in consideration of hardware properties and limitations.

□ The process of T and  $V_R$  is to convert the normalized photon counts to T and  $V_R$  through integration, iteration or looking-up table methods.

□ The process of  $n_c$  is to convert the normalized photon counts to meaningful number density, in combination with prior acquired knowledge or model knowledge of certain atmosphere information or atomic/molecular spectroscopy.

□ These processes sometimes involve considerable binning, smoothing, or temporal integration in order to improve the signal-to-noise ratio (SNR) to result in meaningful results.